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1. A ball is shot (by a pitching machine) from horizontal ground. It reaches the highest point after 3.2 seconds.

(a) What is the height $H$ of the highest point? [5]
(b) The highest point is exactly above the point which is $D=100 \mathrm{~m}$ horizontally away from the starting point as in the figure. What is the initial angle $\theta$ ? [If you are not sure about your answer to (a), find $\tan \theta$ in terms of $H$ and $D$.] [Hint. Try to obtain the $x$-component $v_{x}$ and $y$-component $v_{y}$ of the initial velocity in terms of $D$ and $H$, respectively.] [5]
2. Two masses $m$ and $M$ are connected with a massless string and hang from a massless and frictionless pulley as illustrated below.

(a) Suppose $m=M / 2$. What is the magnitude $a$ of the acceleration of the blocks? Give the value of $a / g$, where $g$ is the acceleration due to gravity. [5]
(b) Suppose $M$ is much larger than $m$ (say, $M=10^{4} m$ ). What is the magnitude $a$ of the acceleration of $m$ ? [5]

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1. A block of mass $m$ is on a rough and horizontal table with coefficient of kinetic friction $\mu_{k}=0.2$ and is connected to another block of mass $M$ via a massless string through a massless and frictionless pulley as shown below.

(a) Suppose $m=M / 2$. What is the magnitude of the acceleration $a$ of the block of mass $m$ on the table? Give the ratio $a / g$, where $g$ is the acceleration due to gravity. [5]
(b) Suppose $M$ is much larger than $m$ (say, $M=10^{4} m$ ). What is the ratio $a / g$ just discussed? You must justify your answer. [2]
2. At the moment when a ball is gently released from $P$, you shoot another ball from $O$ aiming at the ball at P . The point P is exactly above the point that is $L=3 \mathrm{~m}$ horizontally away from you as illustrated. The line connecting O and P makes an angle of $30^{\circ}$ with the horizontal.

(a) The two balls collide at the cross-mark, which is $D=4.9 \mathrm{~m}$ below P. Find the initial speed $V$. [Hint. First, try to calculate the $x$-component $V_{x}$ of the initial velocity.] [5]
(b) Suppose you do the same experiment on a planet whose acceleration of gravity is one half that on earth (i.e., $g / 2$ ). To keep the $L$ and $D$, what is the new initial speed $V^{\prime}$ ? Obtain $V^{\prime} / V$. [5]

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1. At the moment when a ball is gently released from $P$, you throw another ball from $O$ aiming at the ball at P . The point is exactly above the point that is $L=5 \mathrm{~m}$ horizontally away from you as illustrated. The line, which is the direction of the initial velocity, connecting O and P , makes an angle of $30^{\circ}$ with the horizontal.

(a) Obtain the $x$-component of the initial velocity of the ball you throw. [5]
(b) What is the speed of the ball you throw when it hits the other ball? [5]
2. On a frictionless slope that makes an angle $\theta=35^{\circ}$ with the horizontal is a block of mass $m$, which is connected to another identical block of mass $M$ with a massless string through a massless and frictionless pulley as illustrated below.

(a) Suppose $m=M$. What is the magnitude of the acceleration of the blocks?[5]
(b) Suppose $M$ is much larger than $m$ (say, $M=10^{4} m$ ). What is the acceleration of the block of mass $m$ ? [5]

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1. We wish to aim at the target on the wall that is $L=15 \mathrm{~m}$ away at a height of $H=$ $L / 2=7.5 \mathrm{~m}$. You throw a ball with an initialvelocity of $\boldsymbol{V}=\left(V_{x}, V_{y}\right)$.


What is the initial speed $V=|\boldsymbol{V}|$ ? Let us solve this in two parts.
(a) In terms of the $x$-component $V_{x}$ of the initial velocity, it takes the ball $t=L / V_{x}$ to reach the wall. Using this time, write down $H$ in terms of the $x$-component of the initial velocity $V_{x}\left(=V_{y}\right), L$ and the acceleration due to gravity $g$. [5]
(b) Obtain $V_{x}$ and then $V$. [5]
2. On frictionless slopes are two blocks of mass $M$ and of mass $m$ as illustrated below. They are connected by a massless cord through a massless and frictionless pulley.

horizontal
(a) Suppose $m=M$. What is the magnitude of the acceleration of the blocks? [5]
(b) Suppose $M$ is much larger than $m$ (say, $M=10^{4} m$ ). What is the magnitude of the acceleration of the block of mass $m$ ? [5]

